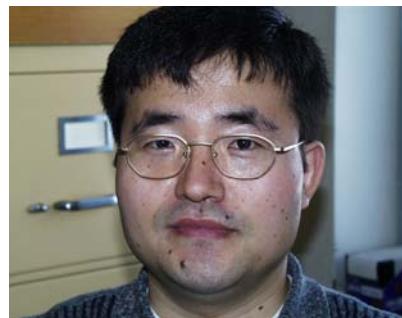


# Workshop on Novel Aspects of Superconductivity

Aspen, 31 July 2007

André-Marie Tremblay

# Antiferromagnetism vs d-wave superconductivity: Insights from the organics

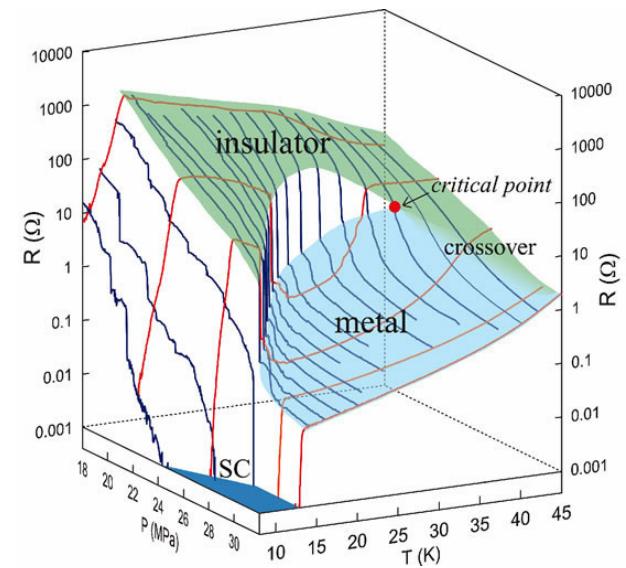
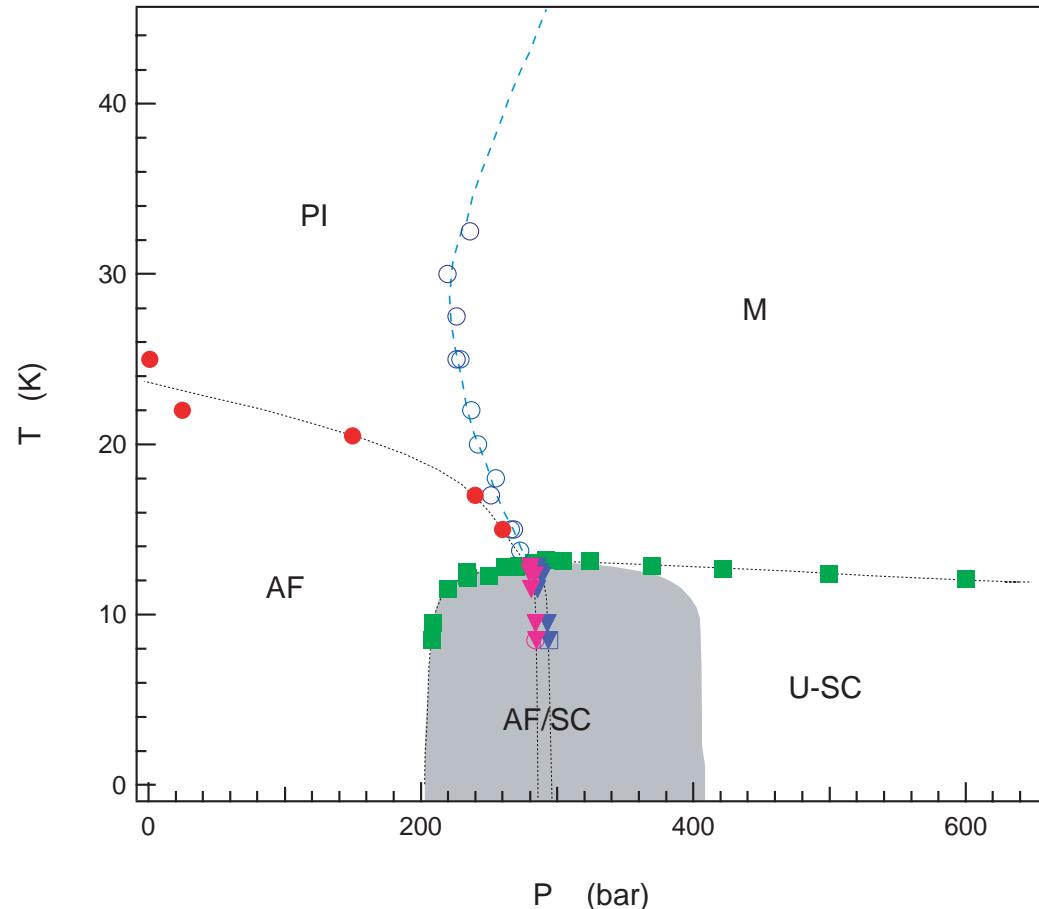


B. Kyung, A.-M. Tremblay,  
Université de Sherbrooke



# Motivation

# Experimental phase diagram for $\kappa$ -BEDT X



F. Kagawa, K. Miyagawa, + K. Kanoda  
PRB **69** (2004) +Nature **436** (2005)

Phase diagram ( $X = \text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$ )

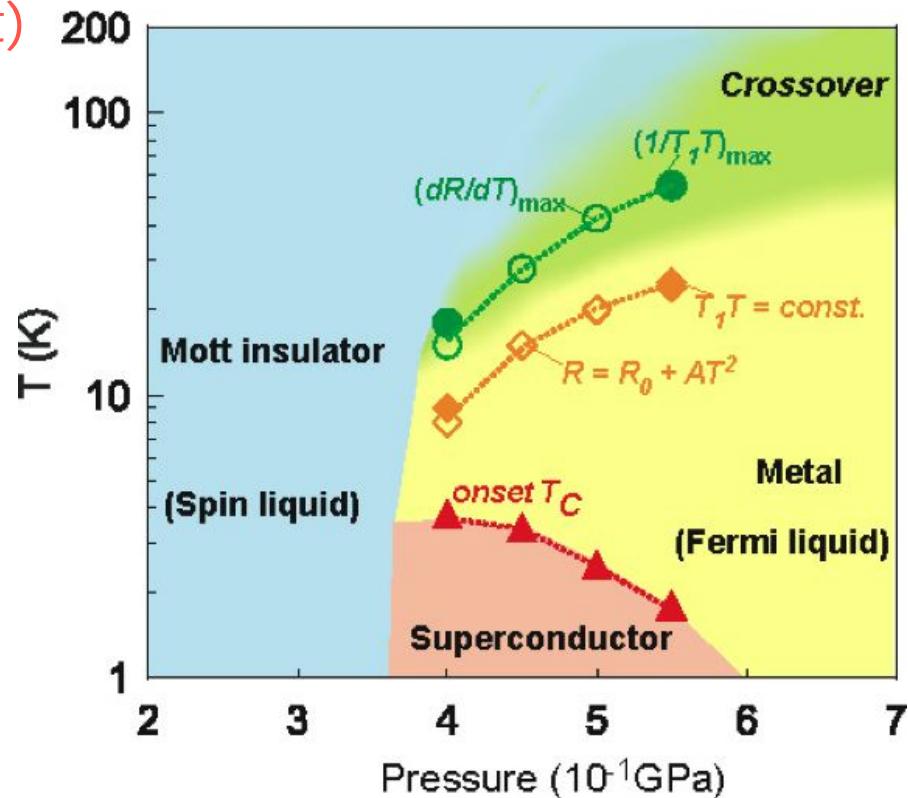
S. Lefebvre et al. PRL **85**, 5420 (2000), P. Limelette, et al. PRL **91** (2003)

# Proposal for AFM mediated d-wave superconductivity

- J. Schmalian PRL **81**, 4232 ('98);
- Kino + Kotani, JPSJ **67**,3691 ('98),
- Kondo + Moriya, JPSJ **67**,3695 ('98)
- M. Vojta +E. Dagotto, PRB, **59**, 713 ('99)

# A spin liquid?

X= Cu<sub>2</sub>(CN)<sub>3</sub> (t'~ t)

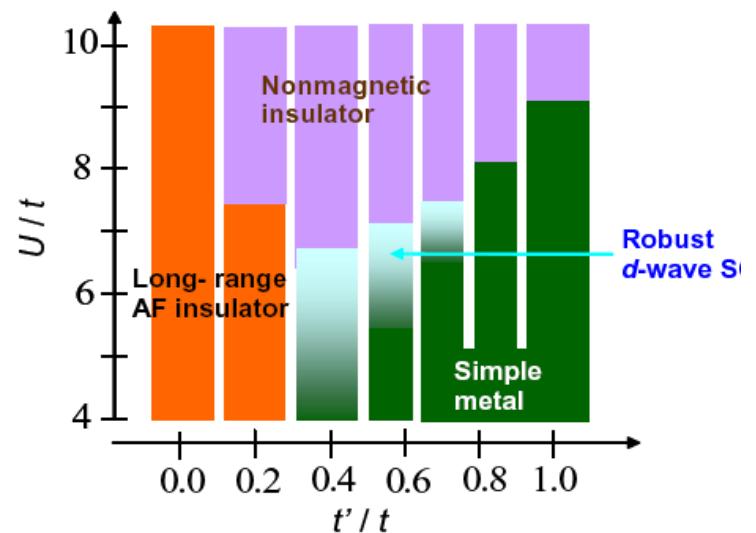


Y. Kurisaki, et al.  
Phys. Rev. Lett. **95**, 177001(2005)

Y. Shimizu, et al. Phys. Rev. Lett. **91**, (2003)

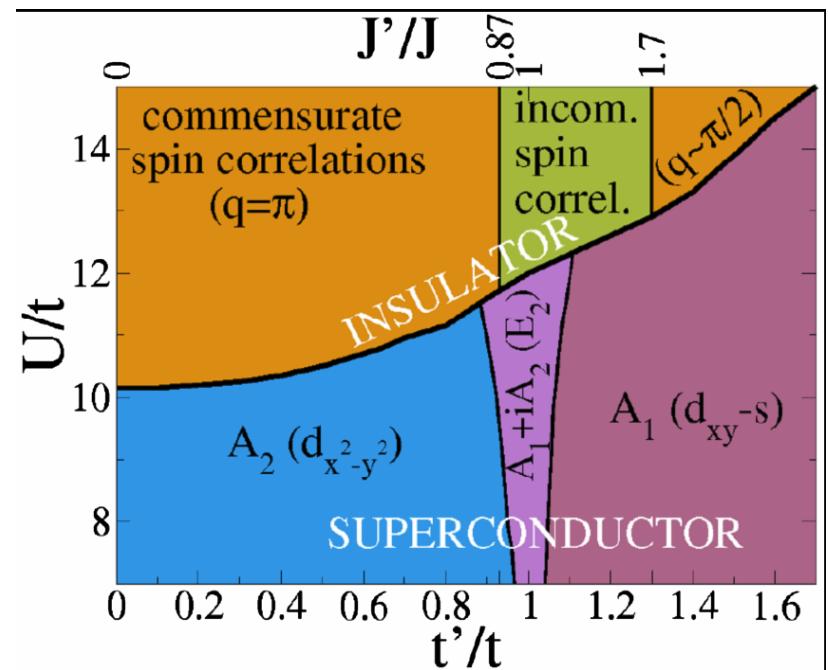
# References on layered organics

- H. Morita, M. Imada et al., J. Phys. Soc. Jpn. 71, 2109 (2002). (PIRG)
- J. Liu, J. Schmalian, et al., Phys. Rev. Lett. 94, 127003 (2005). (VQMC)
- S.S. Lee, P.A. Lee, Phys. Rev. Lett. 95, 036403 (2005). (U(1) gauge)
- B. Powell et al., Phys. Rev. Lett. 94, 047004 (2005). (RVB)
- J.Y. Gan et al., Phys. Rev. Lett. 94, 067005 (2005). (Gossamer)
- T. Watanabe et al., J. Phys. Soc. Japan **75**, 074707 (2006). (VQMC)

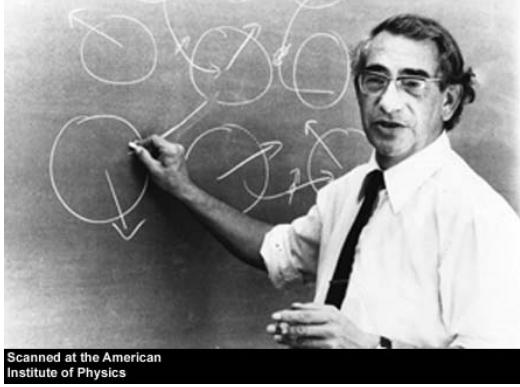


# Recent issues

- Powell BJ, McKenzie RH  
PRL **98**, 027005 (2007).



- Lee SS, Lee PA, Senthil T, PRL **98**, 067006 (2007).
  - Amperean pairing instability in the  $U(1)$  spin liquid state
- V. Galitski, Y.-B. Kim
  - Spin-triplet pairing instability

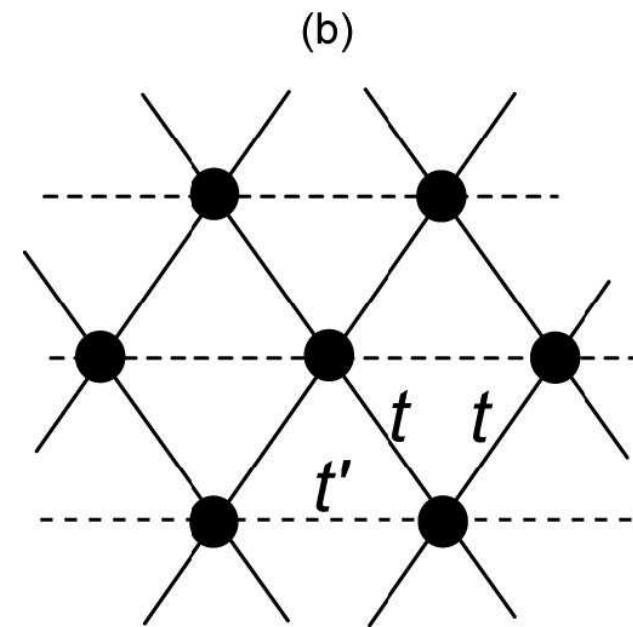
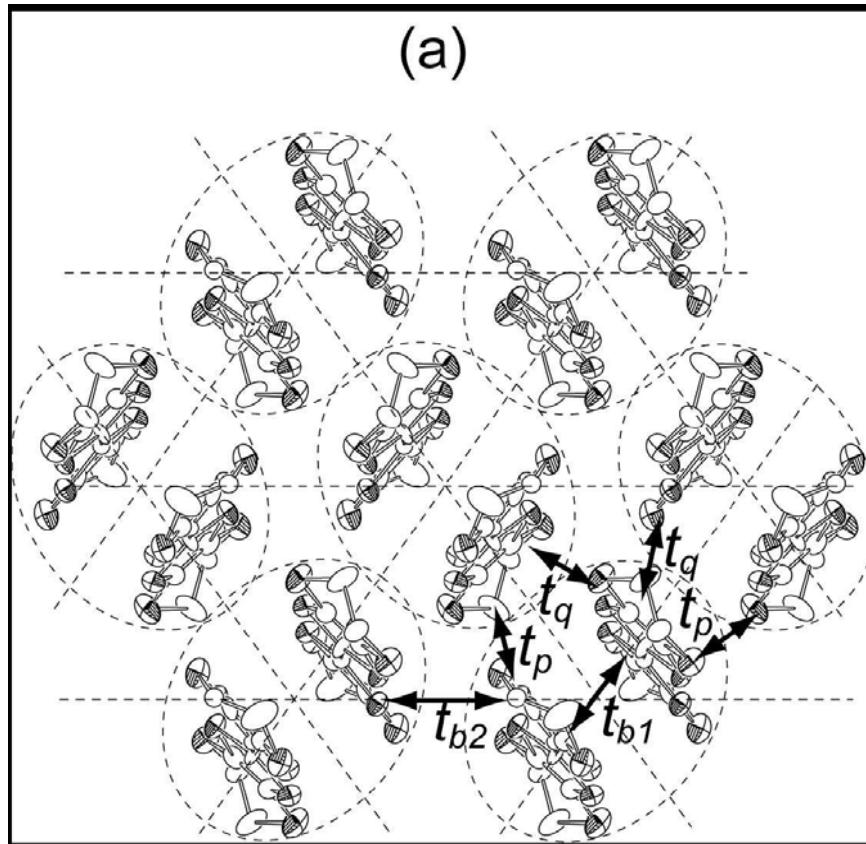


# One-band Hubbard model

$$H = -\sum_{\langle ij \rangle \sigma} t_{i,j} (c_{i\sigma}^\dagger c_{j\sigma} + c_{j\sigma}^\dagger c_{i\sigma}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

# One-band Hubbard model for BEDT organics

H. Kino + H. Fukuyama, J. Phys. Soc. Jpn **65** 2158 (1996),  
R.H. McKenzie, Comments Condens Mat Phys. **18**, 309 (1998)



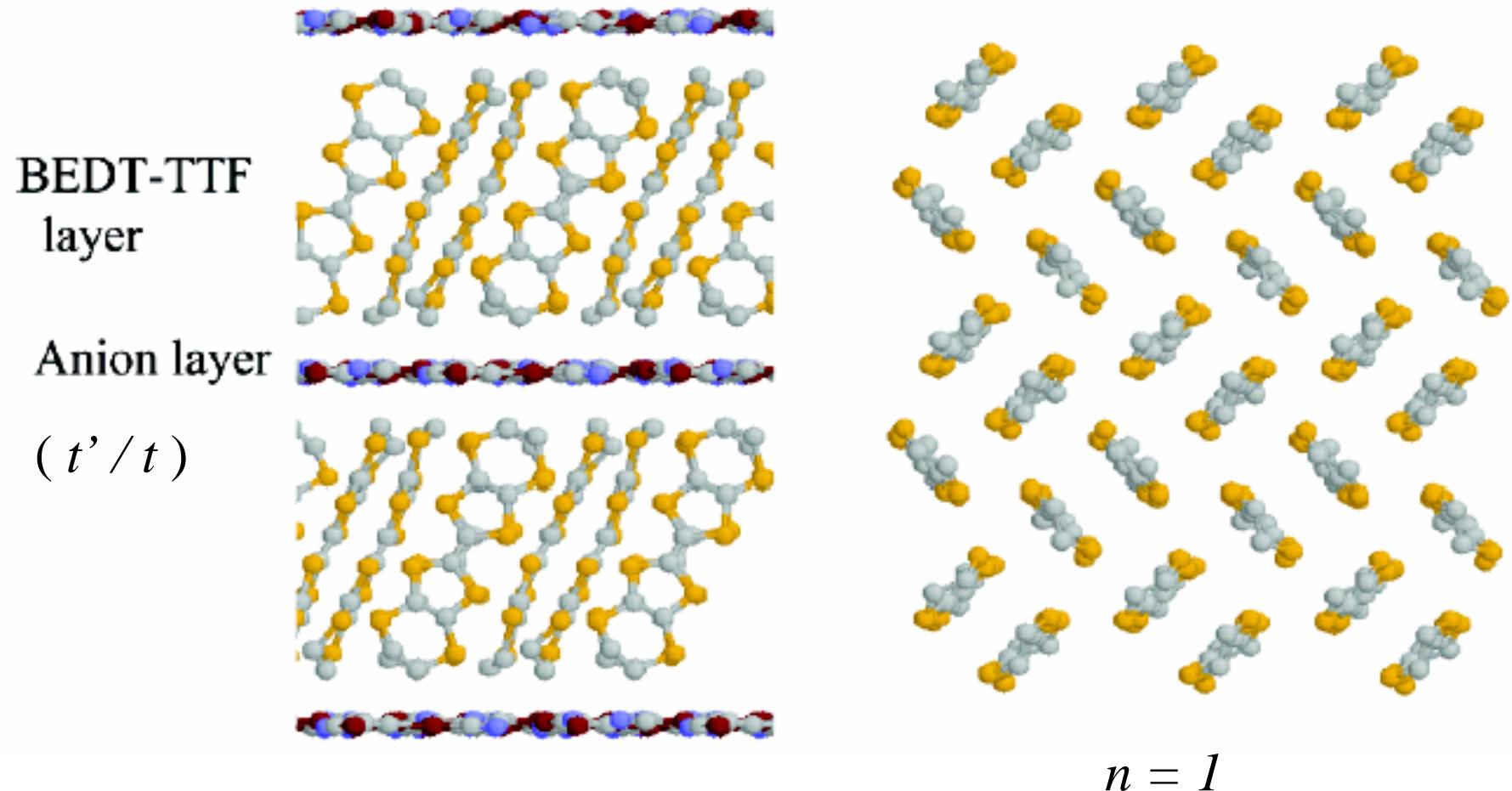
$$t \approx 50 \text{ meV}$$

$$\Rightarrow U \approx 400 \text{ meV}$$

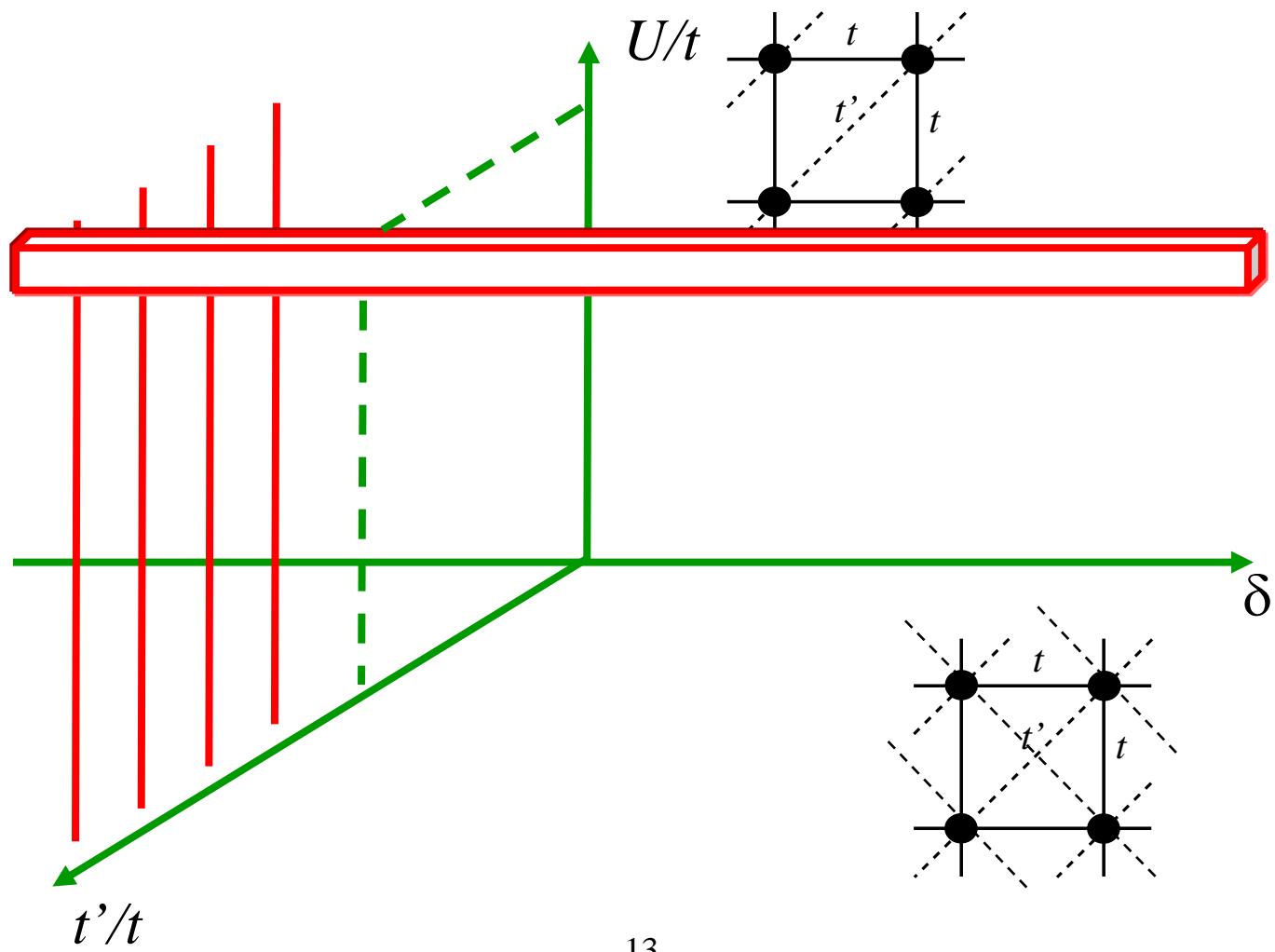
$$t'/t \sim 0.6 - 1.1$$

Y. Shimizu, et al. Phys. Rev. Lett. **91**,  
107001(2003)

# Layered organics ( $\kappa$ -BEDT-X family)

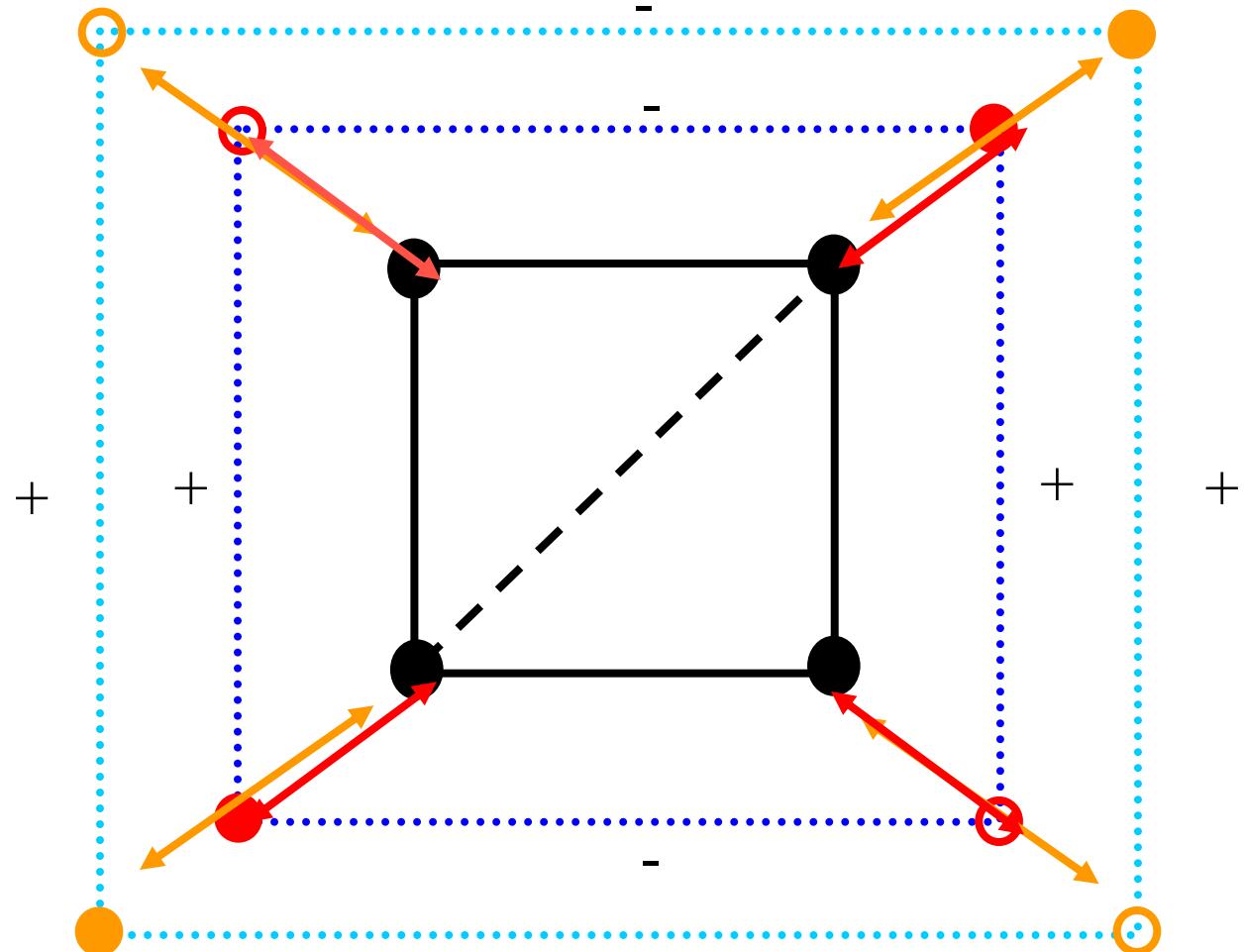


# Perspective



# Methodology

# CDMFT + ED



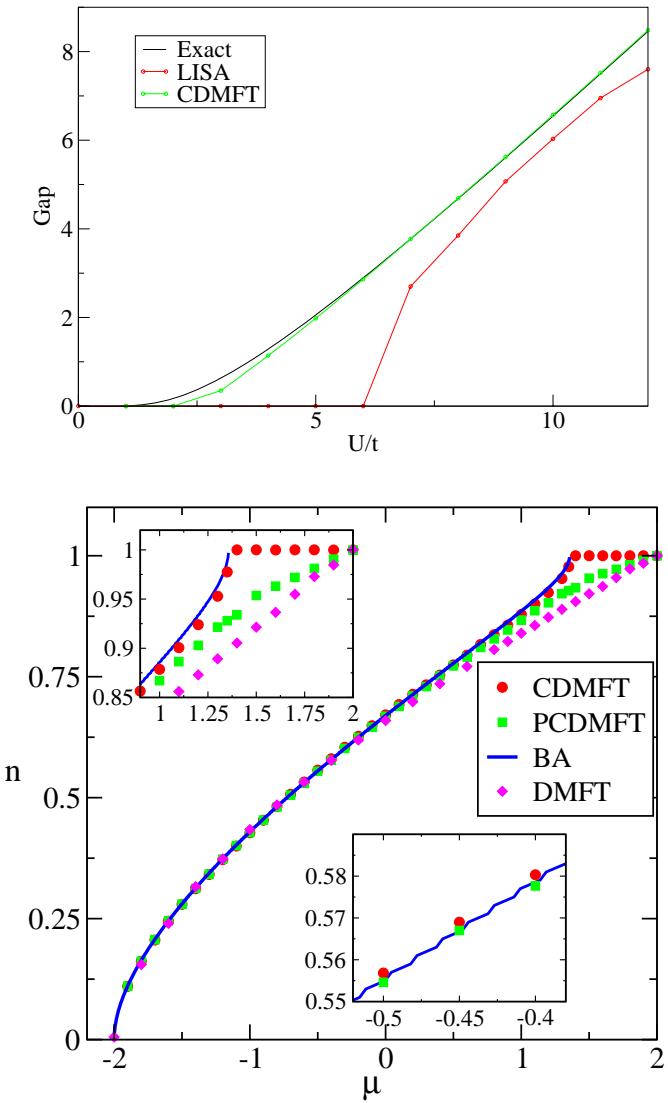
Caffarel and Krauth, PRL (1994)

No Weiss field on the cluster!  
19  
U is never factorized

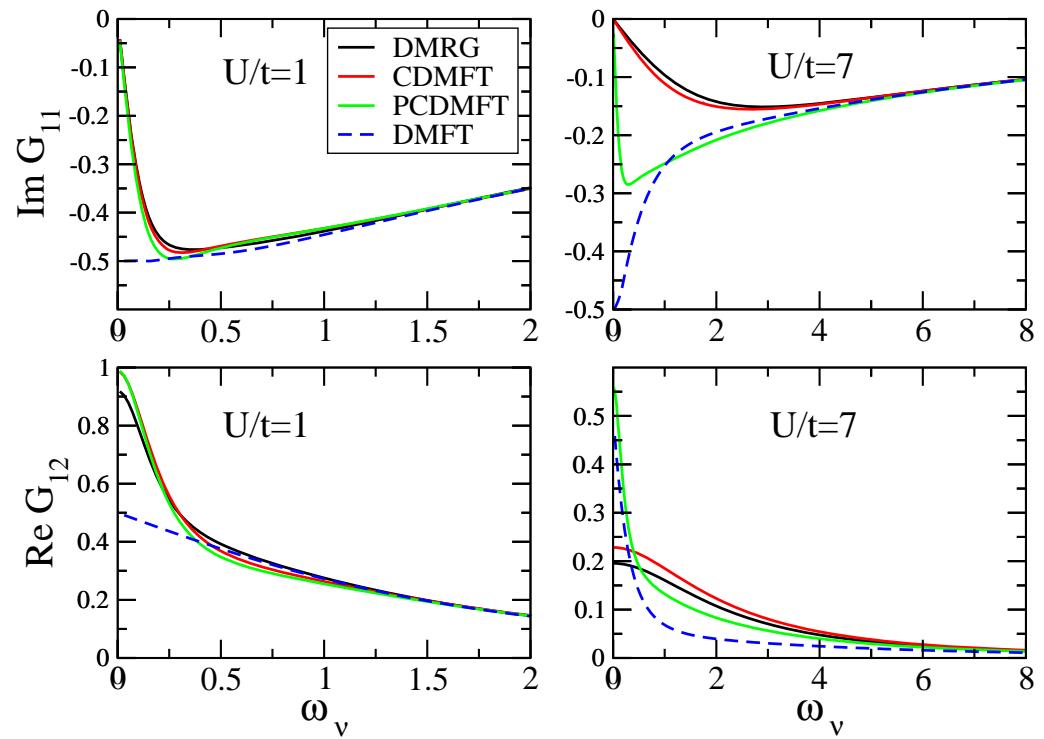


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# Tests : CDMFT



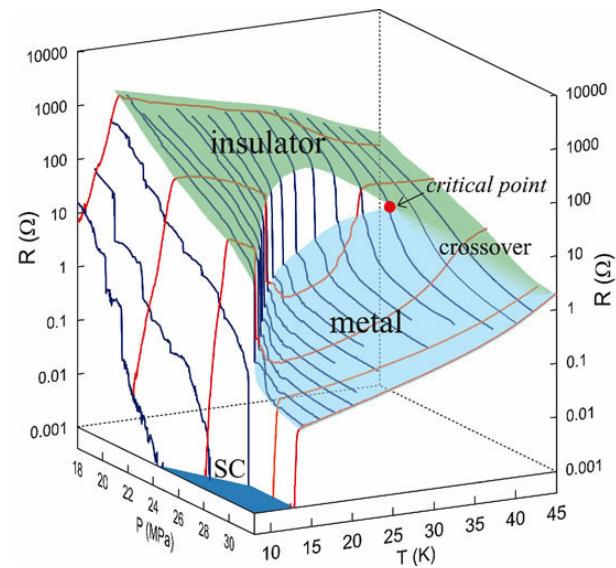
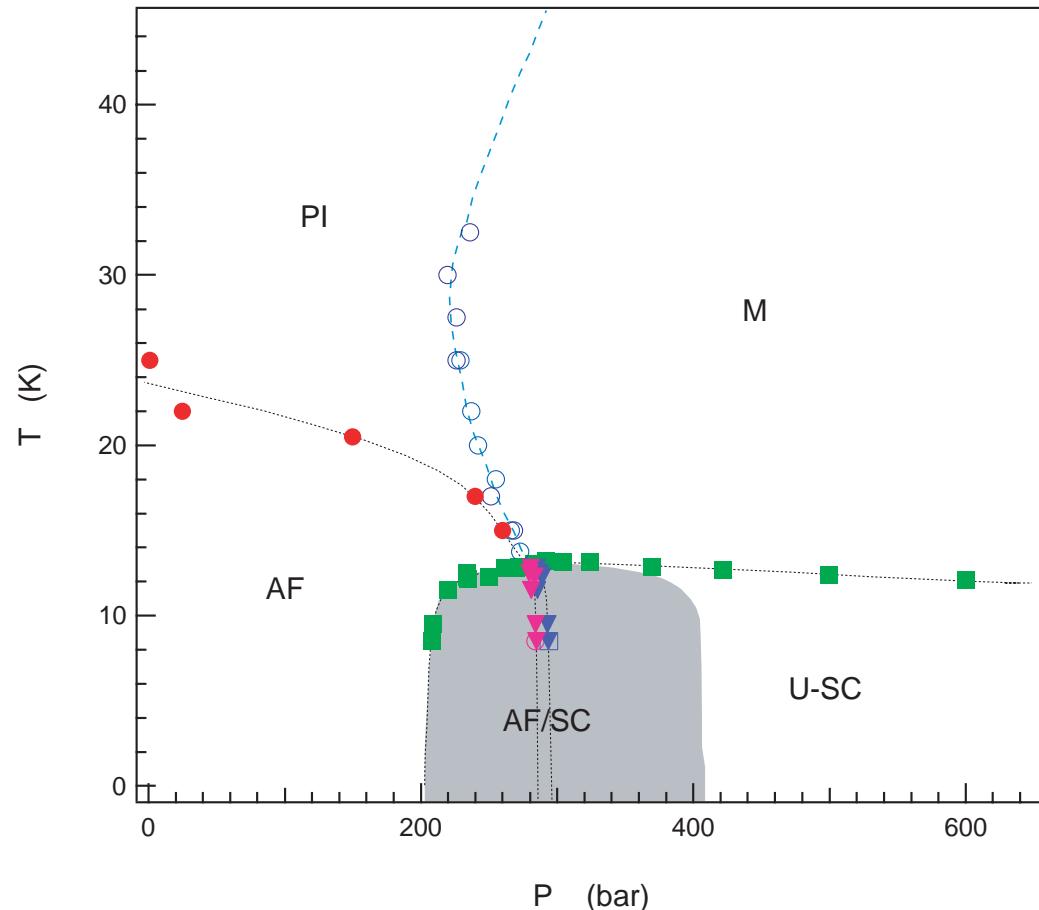
1D Hubbard model: Worst case scenario



Excellent agreement with exact results in both  
metallic and insulating limits  
Capone, Civelli, SSK, Kotliar, Castellani PRB  
(2004)

# Results

# Experimental phase diagram for Cl anions

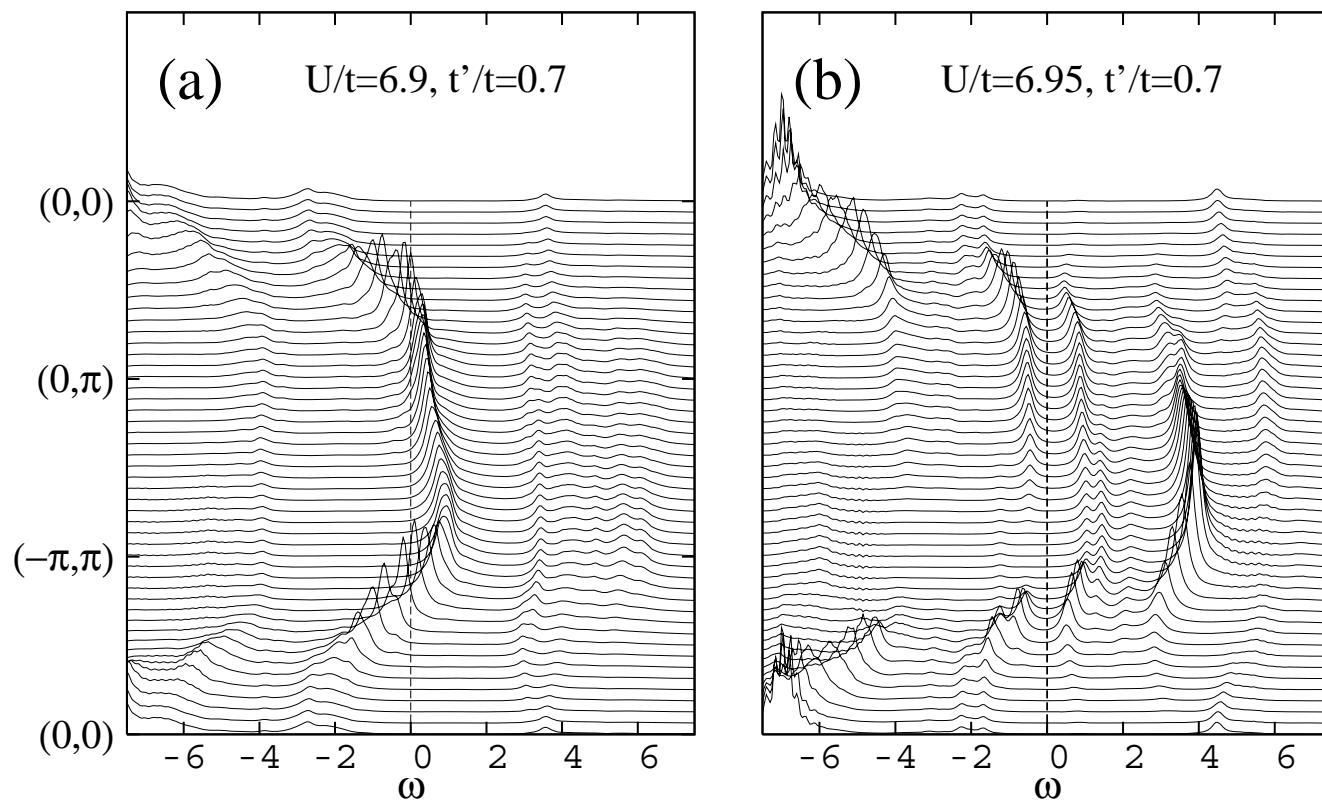


F. Kagawa, K. Miyagawa, + K. Kanoda  
PRB **69** (2004) +Nature **436** (2005)

Phase diagram ( $X=\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$ )

S. Lefebvre et al. PRL **85**, 5420 (2000), P. Limelette, et al. PRL **91** (2003)

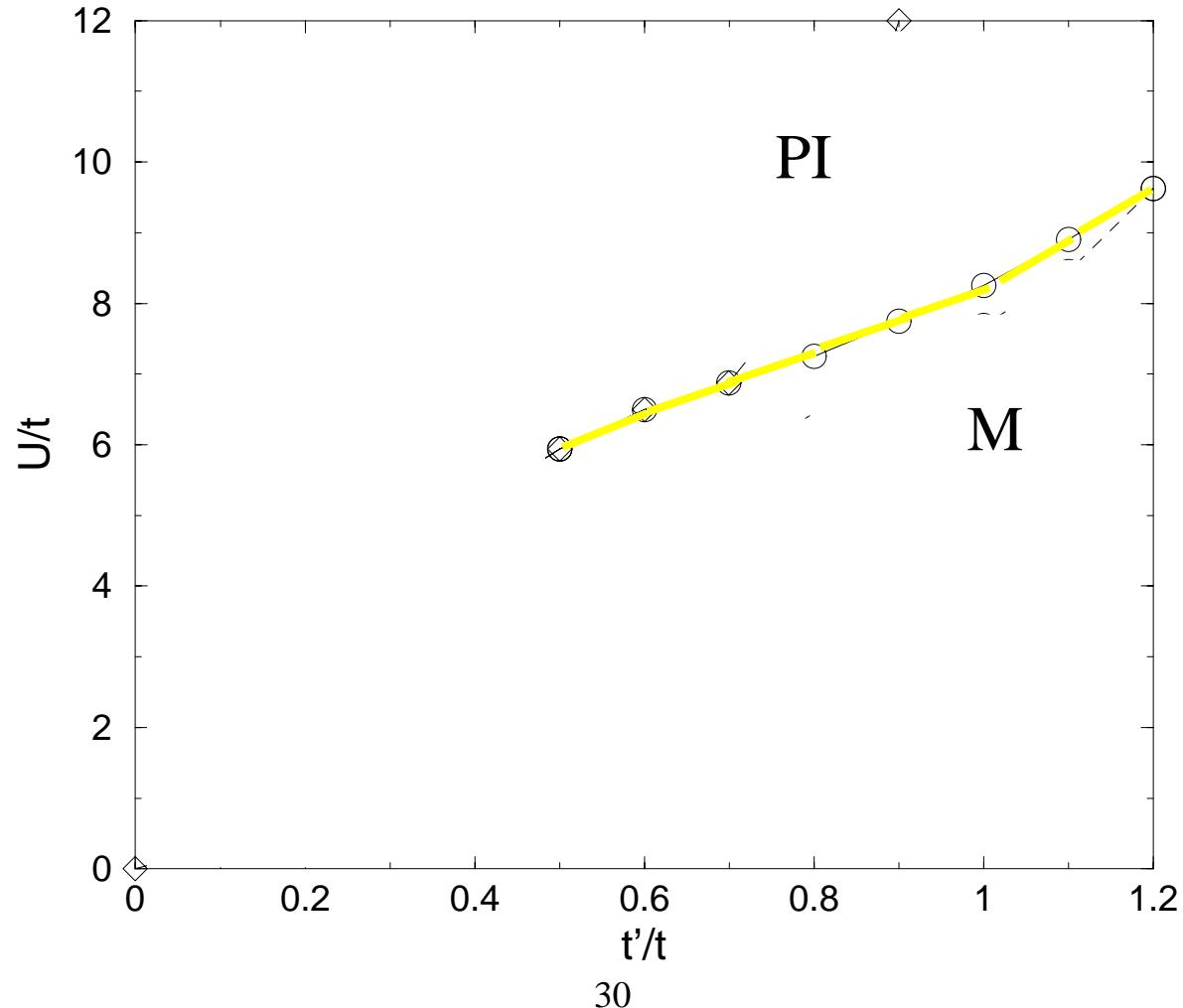
# Mott transition (C-DMFT)



Kyung, A.-M.S.T. PRL (2006)

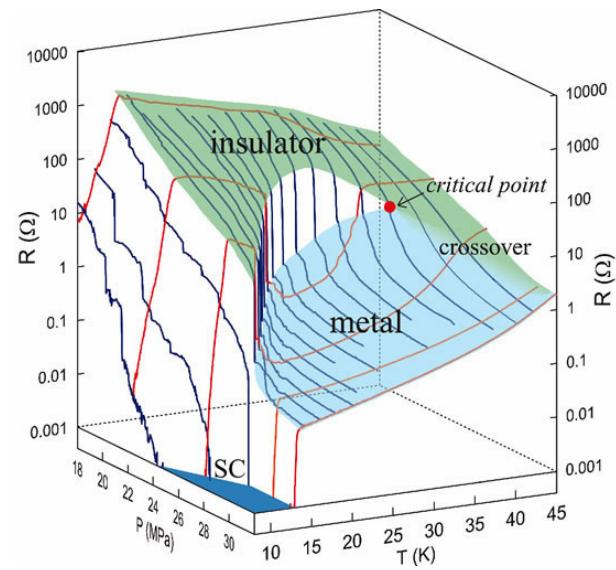
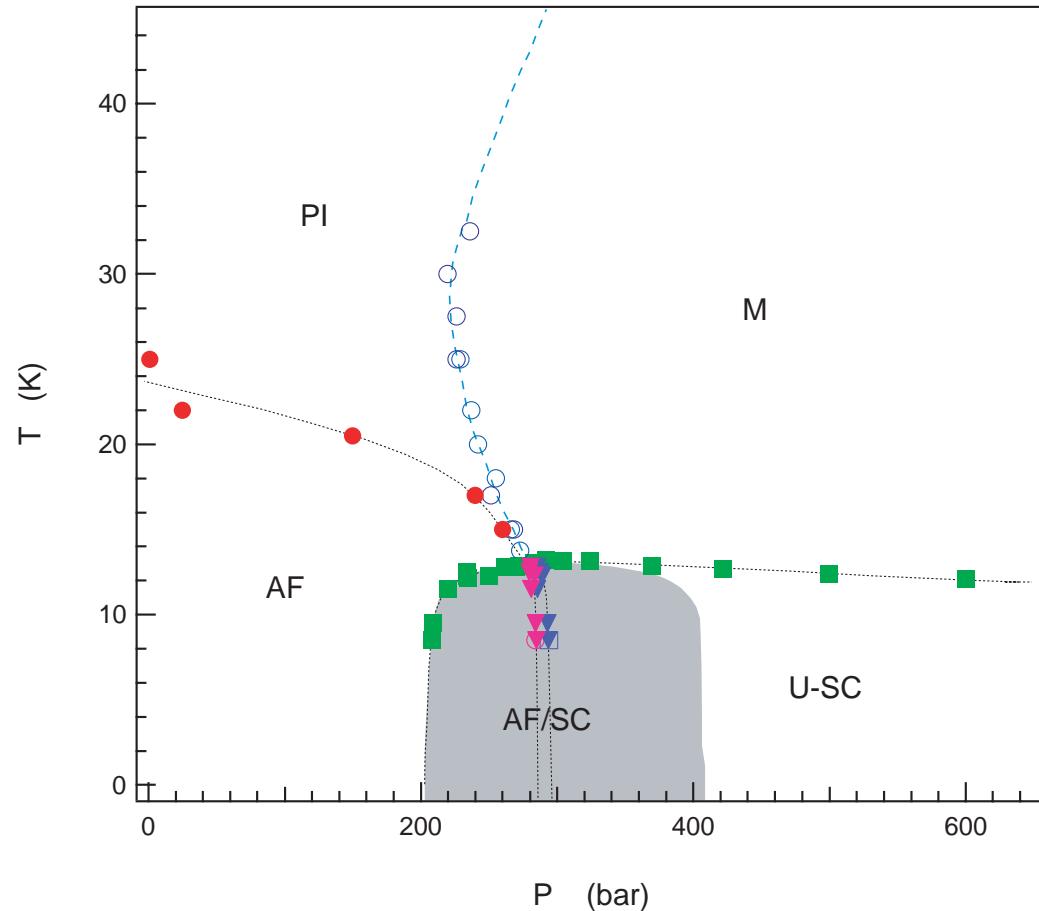
See also, Sénéchal, Sahebsara, PRL (2006)

# Normal phase theoretical results for BEDT-X



Kyung, A.-M.S.T. PRL (2006)

# Experimental phase diagram for Cl anion



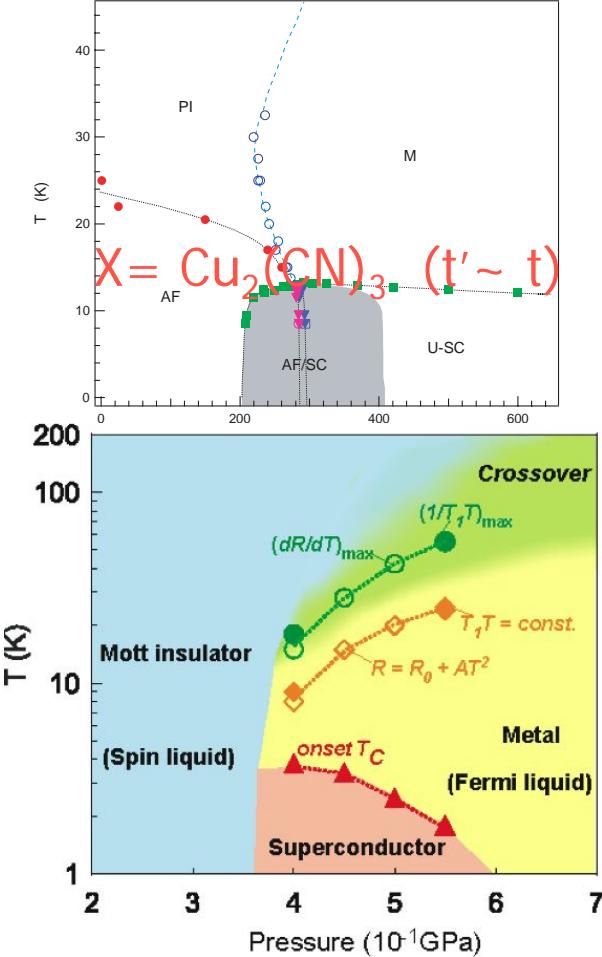
F. Kagawa, K. Miyagawa, + K. Kanoda  
PRB **69** (2004) +Nature **436** (2005)

Phase diagram ( $X=\text{Cu}[\text{N}(\text{CN})_2]\text{Cl}$ )

S. Lefebvre et al. PRL **85**, 5420 (2000), P. Limelette, et al. PRL **91** (2003)

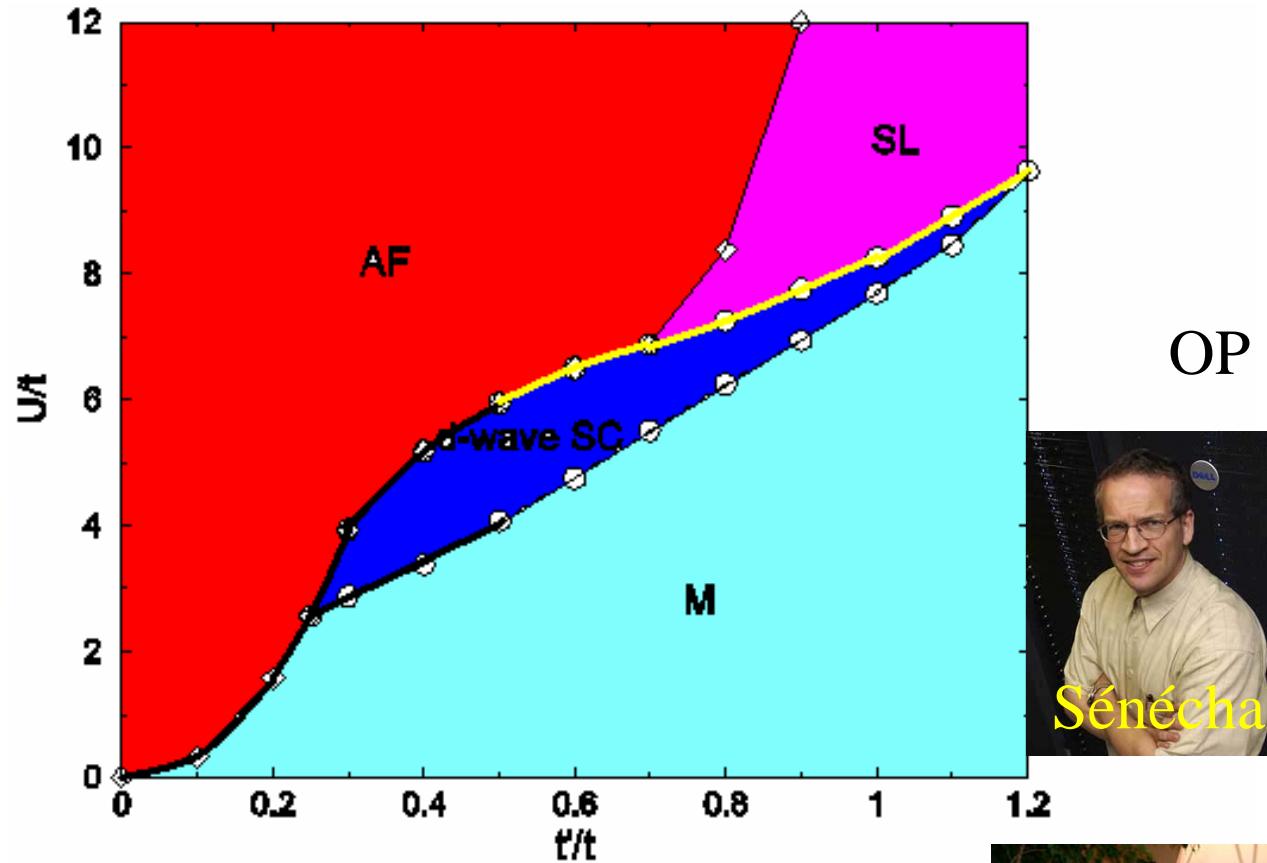


# Theoretical phase diagram BEDT



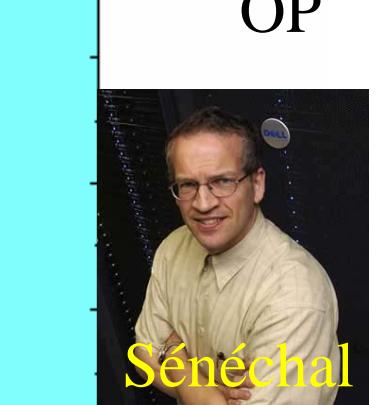
Y. Kurisaki, et al.

Phys. Rev. Lett. **95**, 177001(2005)



Kyung, A.-M.S.T. PRL (2006)

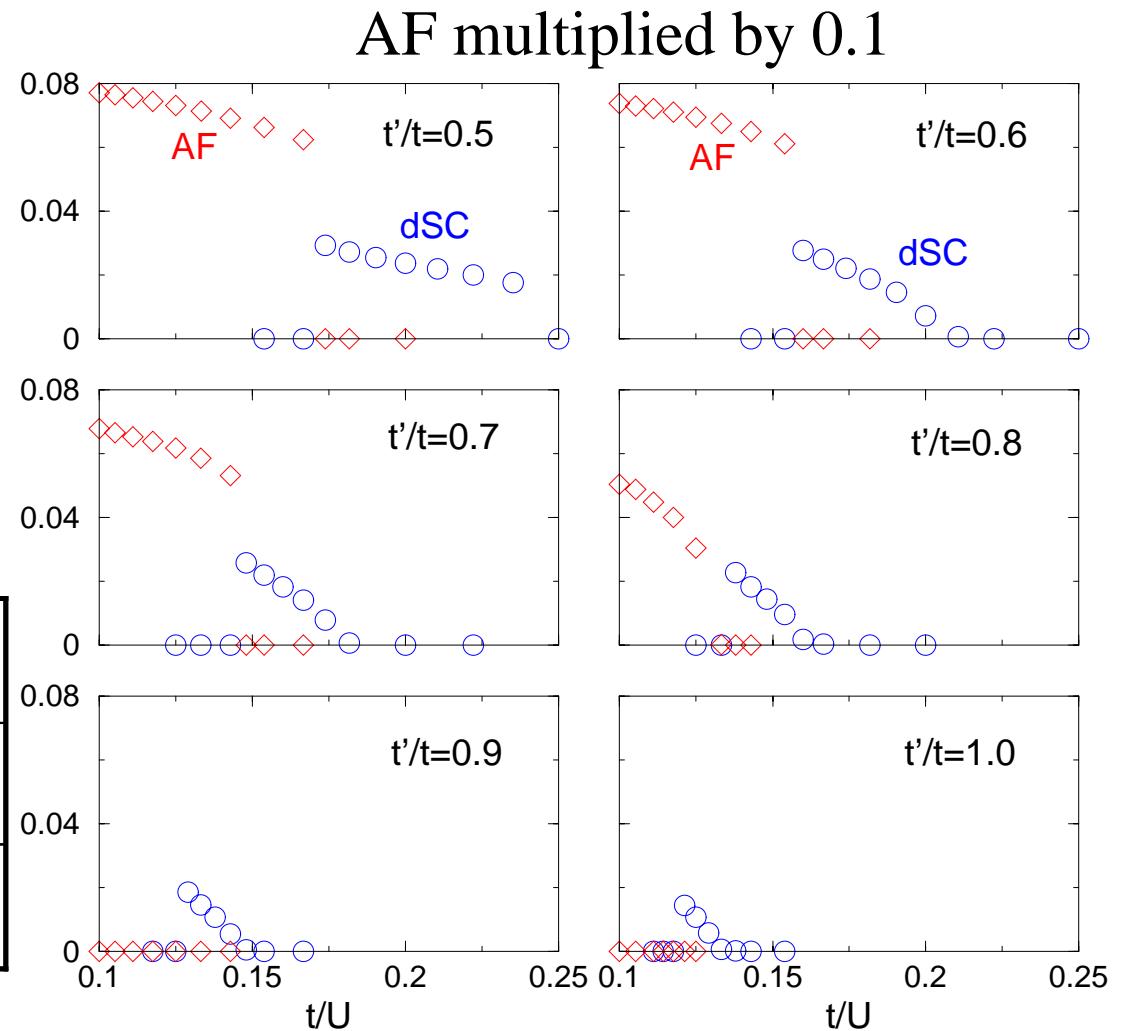
Sénéchal, Sahebsara, PRL 97, 257004 (2006)



# AFM and dSC order parameters for various $t'/t$

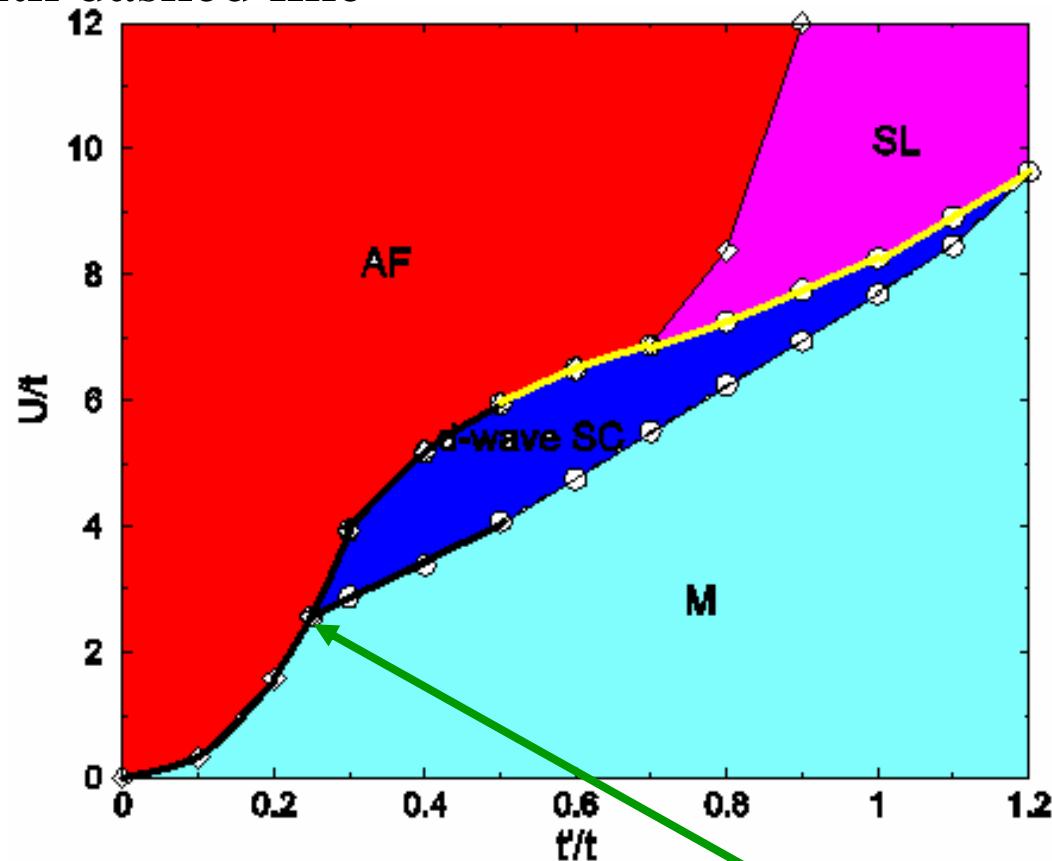
- Discontinuous jump
- Correlation between maximum order parameter and  $T_c$

X	$\text{Cu}[\text{N}(\text{CN})_2]\text{Br}$	$\text{Cu}(\text{NCS})_2$	$\text{Cu}_2(\text{CN})_3$
$t'/t$	0.68	0.84	1.06
$T_c$	11.6	10.4	3.9



# d-wave

- All transitions first order, except one with dashed line

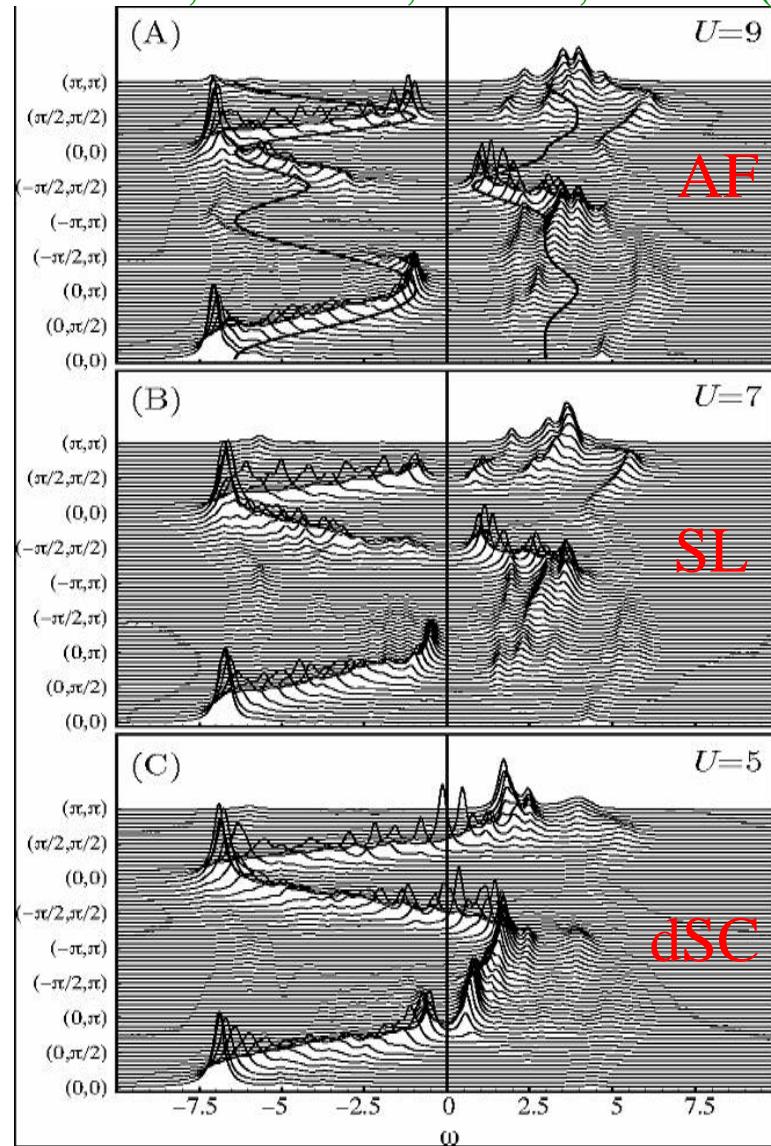


Kyung, A.-M.S.T. PRL 97, 046402 (2006)  
Sénéchal, Sahebsara, PRL 97, 257004 (2006)

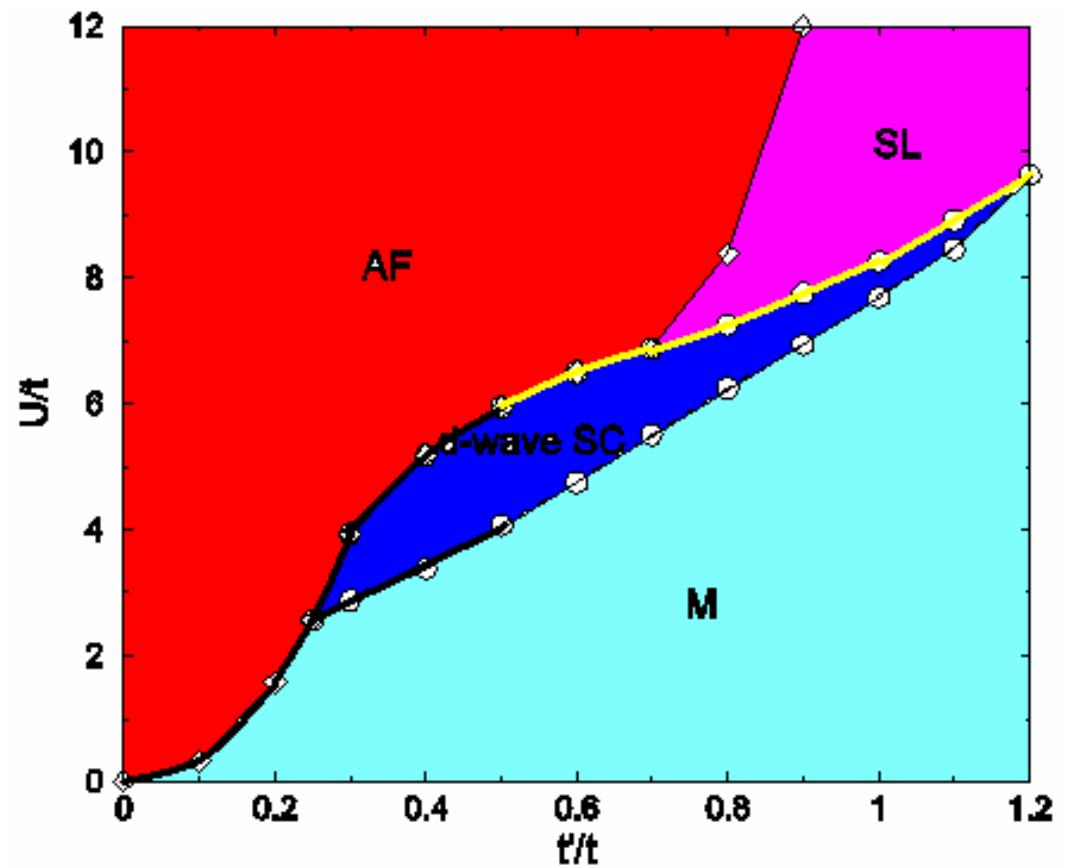
- Triple point, not  $SO(5)$

# Prediction of a new type of pressure behavior

Sénéchal, Sahebsara, PRL 97, 257004 (2006)

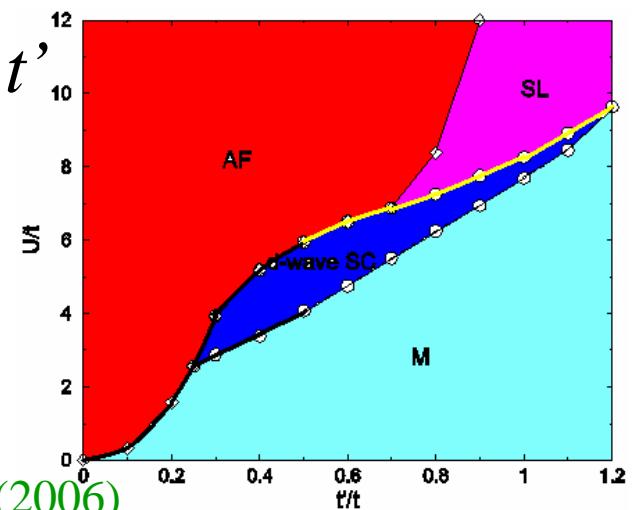


Kyung, A.-M.S.T. PRL (2006)

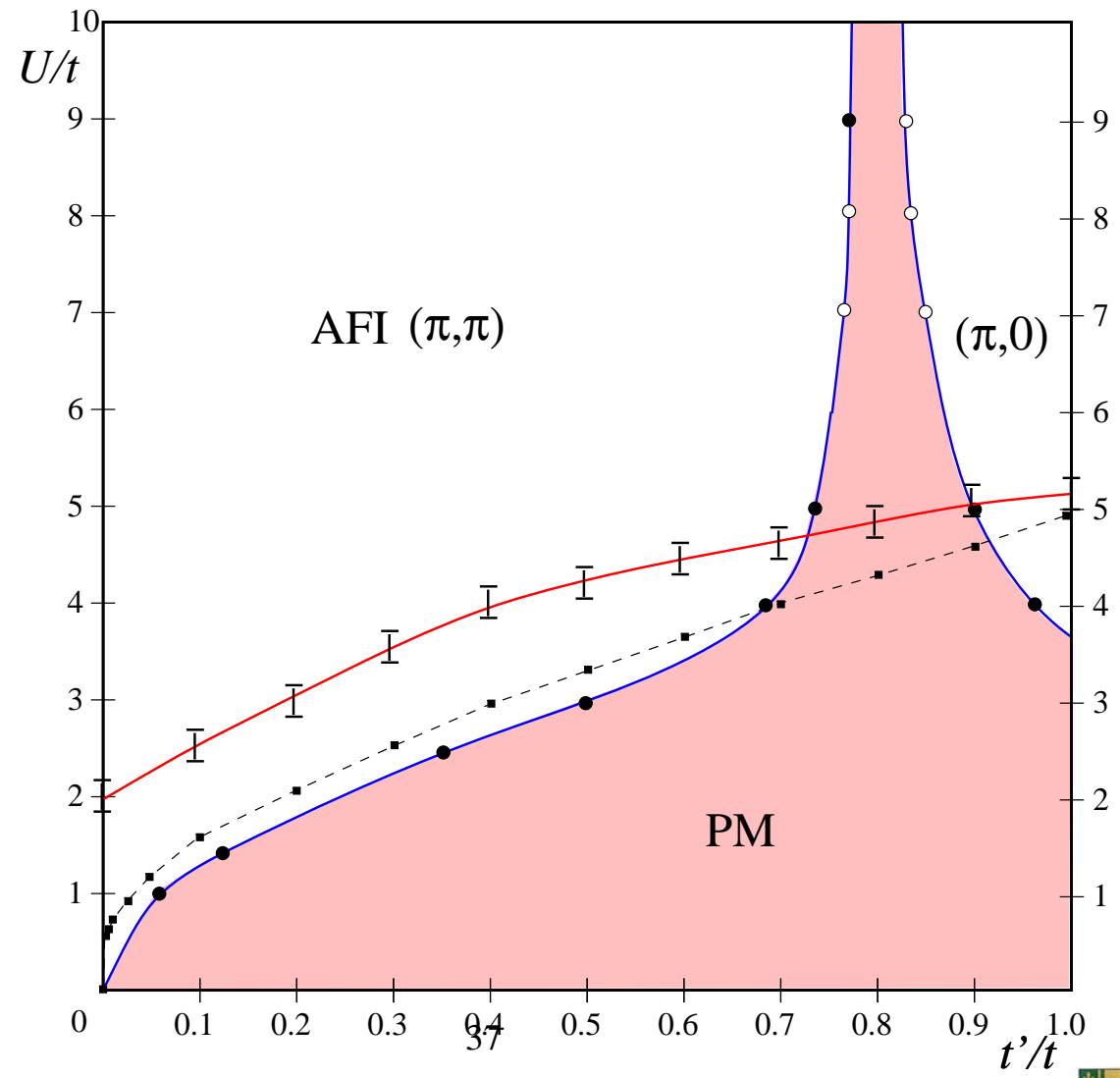
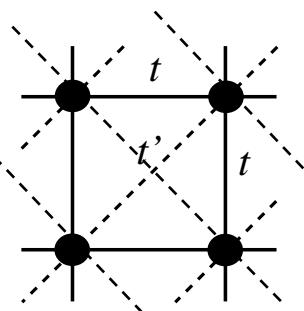


# Conclusion

- One-band Hubbard model on anisotropic triangular lattice contains main experimental features of layered organics:
  - Mott transition in normal state
  - First-order transition between AFM and d-SC or between SL and d-SC depending on frustration
  - Order parameter largest at transition
  - d-SC order parameter decreases with  $t'$
- Insights on d-SC, role of  $t'$  and  $J$
- Correct methodology for High  $T_c$



# High-T<sub>c</sub> lattice at half-filling





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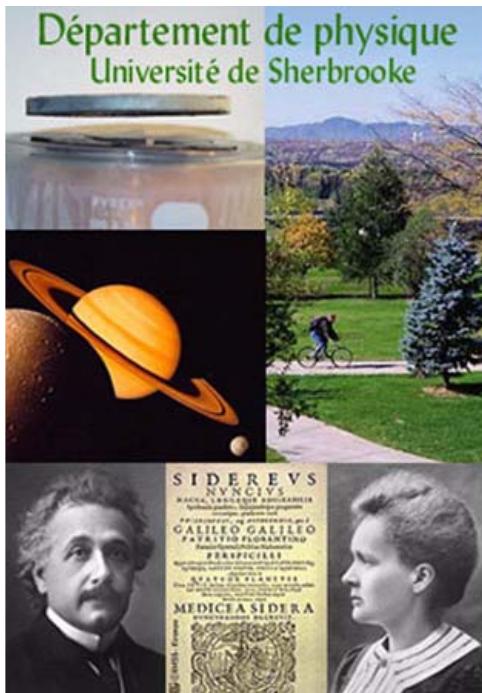


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Le regroupement québécois sur les matériaux de pointe



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Merci