Field-Induced Quantum Critical Point in CeCoIn$_5$

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The resistivity of the heavy-fermion superconductor CeCoIn$_5$ was measured as a function of temperature, down to 25 mK and in magnetic fields of up to 16 T applied perpendicular to the basal plane. With increasing field, we observe a suppression of the non-Fermi liquid behavior, $\rho \sim T$, and the development of a Fermi liquid state, with its characteristic $\rho = \rho_0 + AT^2$ dependence. The field dependence of the T^2 coefficient shows critical behavior with an exponent of 1.37. This is evidence for a field-induced quantum critical point (QCP), occurring at a critical field which coincides, within experimental accuracy, with the superconducting critical field H_{c2}. We discuss the relation of this field-tuned QCP to a change in the magnetic state, seen as a change in magnetoresistance from positive to negative, at a crossover line that has a common border with the superconducting region below ~ 1 K.

The recent discovery of a new family of heavy-fermion superconductors with the general formula CeMIn$_5$ ($M =$ Co, Ir, Rh or their solid solutions) has generated much interest. The ground state of these compounds can be fine-tuned between magnetic order, superconductivity, and a coexistence of the two by varying both pressure and alloy composition [1]. CeCoIn$_5$, with the highest ambient pressure superconducting transition temperature T_c of all heavy-fermion compounds discovered to date [2], is believed to be close to a point where the magnetic state becomes unstable as $T \rightarrow 0$ [3–5]. This proximity to a quantum critical point (QCP) is believed to be responsible for the unusual properties observed in the superconducting [6–10] and normal [11] states.

The peculiar magnetic properties of CeCoIn$_5$ are determined by the magnetic moments of Ce^{3+} ions and by conduction electrons. Through systematic studies of Ce$_{1-x}$La$_x$CoIn$_5$ alloys, where the dilution of magnetic Ce ions by La (nonmagnetic analog) allows one to study the nature of intersite interactions, it has been shown that the energy scales associated with the relevant magnetic interactions are all well separated, and that the dominance of direct intersite interactions below the coherence peak temperature $T_{coh} \sim 50$ K gives rise to pronounced two-dimensional antiferromagnetic (AF) correlations [12]. Although long-range magnetic order is not present in CeCoIn$_5$ [13], the close proximity of this system to AF order [7] results in an abundance of spin fluctuations which lead to behavior that is notably different from that expected in the Fermi liquid (FL) model. In addition to the observation of T-linear resistivity [2] commonly associated with quantum criticality, non-Fermi liquid (NFL) behavior manifests itself in CeCoIn$_5$ in a number of ways. These include a logarithmic increase of the electronic specific heat coefficient on cooling [14], an enhancement of the effective mass at low temperatures and its strong field dependence, as seen in de Haas–van Alphen [15] and microwave conductivity [16] experiments, and a magnetic susceptibility that does not saturate at low temperatures [2].

The close proximity of CeCoIn$_5$ to an AF QCP at ambient pressure offers a unique opportunity to explore quantum critical phenomena in a system free of disorder due to alloying. Since magnetic fluctuations play an essential role in quantum criticality, the response of this system to applied magnetic fields is of clear interest. We have performed a systematic study of the low-temperature electrical resistivity of CeCoIn$_5$ in magnetic fields up to 16 T. We find that this system can indeed be driven through a QCP by a magnetic field, as evidenced by a divergence of the electron-electron scattering strength at the critical field and the subsequent restoration of a FL state. We show that magnetic interactions appear to play a key role in this critical behavior.

Single crystals of CeCoIn$_5$ were grown by the self-flux method [2]. As-grown crystals have a thin platelet shape, with large surfaces corresponding to the (001) basal plane. For this study we have cut four samples into rectangular parallelepipeds with typical dimensions $\sim 2 \times 1 \times 0.3$ mm. Electrical contacts for standard four-wire measurements were made with soldered indium, resulting in ~ 5 mΩ contact resistances. The in-plane electrical resistivity, ρ, was measured with an ac resistance bridge by applying 0.1 mA excitation currents along the basal plane, and transverse magnetic fields up to 16 T parallel to the [001] axis. Measurements were performed from 300 to 0.3 K in a ^{3}He cryostat, and down to 25 mK in a ^{3}He/^{4}He dilution refrigerator. The 16 T data were reproduced in reversed field direction, excluding any spurious Hall component.

On cooling from room temperature, the zero-field resistivity of CeCoIn$_5$ shows a slight increase, followed by a crossover to metallic behavior below T_{coh}, as is seen in many heavy-fermion systems [17]. Below ~ 10 K, $\rho(T)$ displays a linear temperature dependence down to $T_c = 2.3$ K, as shown in Fig. 1(a). Such T-linear behavior has been observed in many systems which lie at or close to a QCP [17,18]. Above 30 K, the magnetoresistance (MR) is negligibly small up to 16 T, whereas below 30 K a notable MR begins to develop as shown in Fig. 1(b). The linear dependence of $\rho(T)$ observed at $H = 0$ suffers a drastic change with increasing field, most pronounced at low temperatures. For instance, the 6 T curve [Fig. 1(a)] displays a notable deviation from linearity below ~ 5 K and decreases on cooling to a value much lower than the residual resistivity inferred from a linear extrapolation of $\rho(T, H = 0)$ to $T = 0$. By 16 T, the downturn in $\rho(T)$ shifts to much higher temperatures [Fig. 1(a)], as evidenced by the large negative MR below ~ 5 K shown in Fig. 1(b). At higher temperatures, the field dependence of ρ, plotted at constant T values in Fig. 1(c), reveals the development of a *crossover* in the sign of MR with increasing field and temperature, which is discussed below.

A close analysis of our 6 T data at low temperatures reveals a narrow but clearly distinguishable range
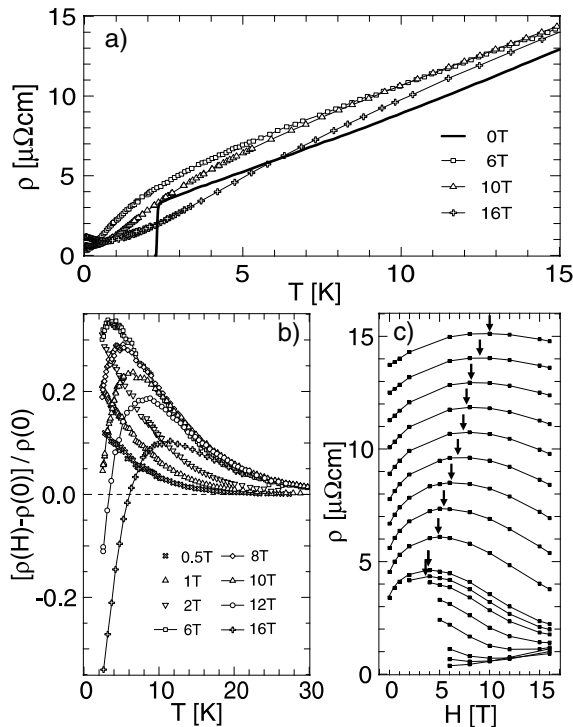
of T^2 behavior below ~ 100 mK, highlighted in a plot of ρ vs T^2 in Fig. 2. This range gradually becomes wider and more apparent with increasing field, as shown by the linear fits [19] in the main panel of Fig. 2, and extends to as high as 2.5 K by $H = 16$ T. Simultaneously, at the lowest measured temperatures, a small *upturn* in $\rho(T)$ starts to develop above 8 T and continues to grow upon further field increase. Since this effect is confined to very low temperatures and high fields, it does not hinder the observation of T^2 resistivity and is left for future study [21].

The behavior of MR in CeCoIn$_5$ can be compared to that observed in two closely related superconductors. In CeIrIn$_5$, no significant MR has been observed between 50 mK and 5 K at ambient pressure [2]. In CeRhIn$_5$, a large positive MR was observed [23] at ambient pressure, while under the critical pressure (where AF order is suppressed and superconductivity is dominant) the low-temperature MR [24] bears a striking similarity to that observed in our study. The development of a T^2 dependence of resistivity was also seen in CeCoIn$_5$ under applied pressure, where a jump in the exponent of T from linear to quadratic occurs near 2 GPa [5]. From these comparisons, it would appear that the Co system at ambient pressure is close to quantum criticality in the same manner as the Rh system under critical pressure, while the Ir system is further from criticality at ambient pressure.

The slope of the fitted ρ vs T^2 curves (Fig. 2), i.e., the coefficient A of the T^2 term (in $\rho = \rho_0 + AT^2$), is a measure of the strength of electron-electron interactions, notoriously high in heavy-fermion materials. As is clear
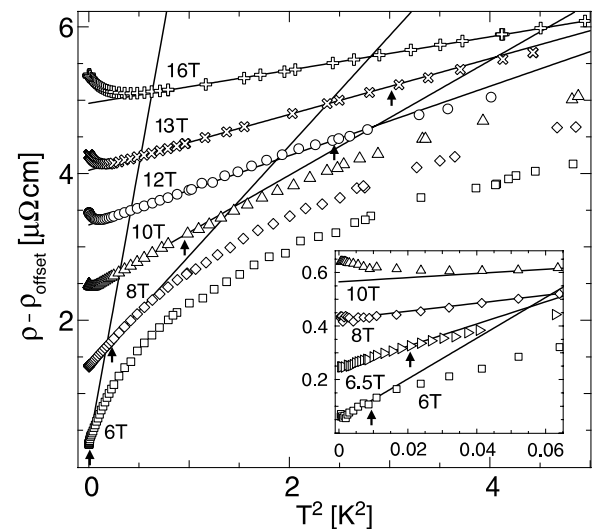

FIG. 1.   Resistivity of CeCoIn$_5$ under various fields, shown (a) for $H = 0$, 6, and 16 T, (b) as magnetoresistance versus temperature, normalized to zero field resistivity, and (c) versus applied field, as isotherms for $T = 16$, 14.5, 13, 11.5, 10, 8.5, 7, 5.5, 4, 2.5, 2.25, 2, 1.5, 1, 0.5, 0.3, and 0.1 K from top to bottom (lines are guides to the eye and are not offset). The arrows in (c) indicate the position of the crossover from positive to negative MR with increasing field for each temperature.

FIG. 2.   Low temperature resistivity of CeCoIn$_5$ plotted vs T^2 for several magnetic fields, with an inset showing low temperature data (data sets are offset for clarity in both figures). The solid lines are linear fits to the data, showing the behavior of the quadratic-term coefficient (slope) under applied field, with arrows indicating the upper limit of the temperature range of T^2 behavior.

from the fits in Fig. 2, A tends to decrease with increasing field. The field dependence of A, or $A(H)$ (inset in Fig. 3), displays *critical* behavior best fitted by the function $A \propto (H - H^*)^\alpha$, with parameters $H^* = 5.1 \pm 0.2$ T and $\alpha = -1.37 \pm 0.1$. In FL theory, the coefficient A is roughly proportional to the square of the electronic contribution to the specific heat coefficient γ. Thus, the critical behavior of $A(H)$ would lead us to expect a divergence of $\gamma(H)$ somewhere close to H_{c2}. Experimental studies of the specific heat at fields slightly exceeding H_{c2} indeed show an increase of $\gamma(H)$ [14].

The field-induced recovery of a FL regime in CeCoIn$_5$ exhibits a distinct similarity to the behavior observed in several other systems. In Sr$_3$Ru$_2$O$_7$ and CeRu$_2$Si$_2$, a field-induced anomaly in resistivity is associated in both cases with a change from predominantly AF to ferromagnetic fluctuations [25]. In U$_{0.9}$Th$_{0.1}$Be$_{13}$ [20], a system close to a superconducting phase, the evolution of $A(H)$ and T^2 resistivity with field both bear a close resemblance to that found in our study. In YbRh$_2$Si$_2$, critical behavior in $A(H)$ was observed in proximity to a field-induced QCP associated with a second-order AF transition, with an exponent $\alpha = -1$ extracted from $A(H)$ that is similar to the value we obtain in CeCoIn$_5$ [26].

All of the aforementioned systems exhibit critical behavior in resistivity when approaching some critical field value H^*. However, what is unique (and intriguing) about CeCoIn$_5$ is the fact that H^* is very close to $H_{c2}(0)$,
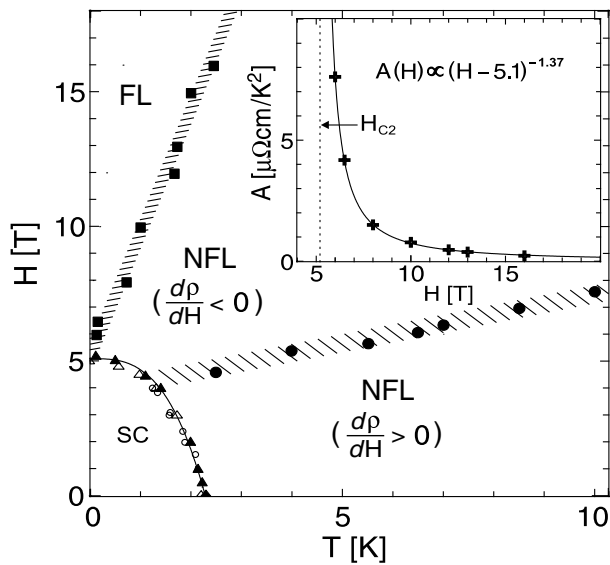
which points to the existence of a QCP coincident with the superconducting transition at $T = 0$. The question is whether this coincidence is essential or accidental. In the latter case, the critical behavior would originate from proximity to an ordered phase (and transition) other than the superconducting state (and, in fact, would be masked by superconductivity). In this respect it is interesting to mention the compelling evidence from magnetization [27,28], specific heat [29], and thermal conductivity [9] that the H_{c2} transition in CeCoIn$_5$ is first order below ~ 0.7 K for all field orientations. This suggests that critical behavior of the kind observed here, which is usually associated with a second-order phase transition brought to absolute zero, is not caused by the vicinity of the superconducting state itself. Rather, it is tempting to propose that the quantum critical behavior observed in CeCoIn$_5$ is associated with a zero-temperature transition of magnetic origin, much as the field-induced transition from an AF state to a field-aligned state in YbRh$_2$Si$_2$.

In connection to this, note that there is a pronounced crossover from positive to negative MR that occurs at high temperatures with increasing field. It is clear that the shape of the $\rho(H)$ curves is notably different from that expected for weak-field orbital MR ($\Delta\rho \sim H^2$), while at high fields the MR becomes negative. Both of these facts encourage us to consider an unconventional magnetic origin to the observed MR behavior. This conclusion is natural, taking into account the connection commonly made between zero-field T-linear resistivity and AF spin fluctuations [17,30]. In this scenario, the initial increase of ρ with field could originate from an increase of spin disorder. Although positive MR is unexpected in Kondo systems [31], an increase of MR with field is indeed observed in systems with AF order [23,26], and in systems approaching a coherent state [32]. In CeCoIn$_5$, there is no evidence for long-range AF order in zero external field. However, notable AF correlations are observed below $T_{\rm coh}$, and therefore it is natural to associate the increase of spin disorder with a suppression of AF correlations. Clearly, the polarization of spins by increasing field strength should eventually lead to a field-aligned state, as was observed in the case of YbRh$_2$Si$_2$ [26]. Therefore, a crossover to negative MR should occur at progressively increasing fields at higher temperatures, which is indeed observed in our experiment.

Based on our experimentally determined ranges of T^2 behavior at low temperatures, and on the crossover observed in the sign of MR at high temperatures, we have constructed a phase diagram of the H-T plane (Fig. 3). It is apparent that the MR crossover line approaches the H_{c2} transition at a finite temperature, so that below ~ 1 K the domain of negative MR is directly adjacent to the superconducting domain. Surprisingly, this diagram strongly resembles that determined by torque magnetometry [27] for $H \parallel [110]$, where the jump in torque associated with the first-order H_{c2} transition below ~ 1.4 K was traced

FIG. 3. H-T phase diagram of CeCoIn$_5$ determined from resistivity measurements, including the upper bound of T^2 resistivity (■), the position of the MR maximum (●), and H_{c2} determined by resistivity H and T sweeps (▲), which agrees with specific heat (○) and resistivity (△) measurements from Ref. [2]. The hatched lines indicate the crossover boundaries between FL and NFL (negative and positive MR) regimes, as explained in the text. The inset shows the field dependence of the quadratic coefficient A of $\rho(T)$ [the solid line is a fit of the data points (+) to the displayed formula].

well into the normal state (up to ~25 K), indicative of a metamagnetic transformation. Although no such anomaly was found above T_c for $H \parallel [100]$ or $H \parallel [001]$, and subsequent magnetization measurements did not reproduce this result [28], the sensitivity of torque measurements may highlight the importance of the $H \parallel [110]$ orientation. The similar behavior observed in both MR and torque measurements further suggests the possible existence of a magnetic order parameter, where the direct observation of a transition may be complicated by the emergence of superconductivity.

In conclusion, we have identified the anomalous low-temperature evolution of magnetoresistance in CeCoIn$_5$ with the field-induced development of a Fermi liquid regime. This evolution and the critical nature of the electron-electron scattering coefficient thus derived both bear close resemblance to other systems governed by quantum criticality. The crossover from positive to negative magnetoresistance, which extends to high temperatures, is indicative of a change in character of spin fluctuations with increasing field strength and may be closely tied to the critical behavior observed in the resistivity, hinting at a quantum critical point of a magnetic nature, masked by superconductivity.

Note added.—Recent specific heat measurements by Bianchi *et al.* [33] support our main conclusion regarding the existence of a field-induced QCP.

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[1] P. G. Pagliuso *et al.*, Physica (Amsterdam) **312B**, 129 (2002); P. G. Pagliuso *et al.*, Phys. Rev. B **64**, 100503(R) (2001); V. S. Zapf *et al.*, Phys. Rev. B **65**, 014506 (2001).
[2] C. Petrovic *et al.*, J. Phys. Condens. Matter **13**, L337 (2001).
[3] M. Nicklas *et al.*, J. Phys. Condens. Matter **13**, L905 (2001).
[4] H. Shishido *et al.*, J. Phys. Soc. Jpn. **71**, 162 (2002).
[5] V. A. Sidorov *et al.*, Phys. Rev. Lett. **89**, 157004 (2002).
[6] R. Movshovich *et al.*, Phys. Rev. Lett. **86**, 5152 (2001).
[7] Y. Kohori *et al.*, Phys. Rev. B **64**, 134526 (2001).
[8] N. J. Curro *et al.*, Phys. Rev. B **64**, 180514 (2001).
[9] K. Izawa *et al.*, Phys. Rev. Lett. **87**, 057002 (2001).
[10] R. J. Ormeno *et al.*, Phys. Rev. Lett. **88**, 047005 (2002).
[11] J. L. Sarrao, Int. J. Mod. Phys. B **16**, 3025 (2002).
[12] S. Nakatsuji *et al.*, Phys. Rev. Lett. **89**, 106402 (2002),
and references therein.
[13] W. Higemoto *et al.*, J. Phys. Soc. Jpn. **71**, 1023 (2002).
[14] S. Ikeda *et al.* J. Phys. Soc. Jpn. **70**, 3187 (2001); J. S. Kim *et al.*, Phys. Rev. B **64**, 134524 (2001).
[15] R. Settai *et al.*, J. Phys. Soc. Jpn. **71**, 162 (2002).
[16] S. Özcan *et al.*, Europhys. Lett. **62**, 412 (2003).
[17] See, for example, G. R. Stewart, Rev. Mod. Phys. **56**, 755 (1984); **73**, 797 (2001).
[18] For a review, see P. Coleman *et al.*, J. Phys. Condens. Matter **13**, R7235 (2001); N. D. Mathur *et al.*, Nature (London) **394**, 39 (1998).
[19] The range of T^2 behavior was determined using a procedure identical to that used in Ref. [20]. Linear least-squares fits of the data were made over a varying interval of temperatures, fixing the lower bound at the lowest temperature point and varying the upper temperature bound. The reduced chi-square value was determined for each fit interval and plotted as a function of the upper bound of the fitting range. The upper bound corresponding to the minimum chi-square value was then chosen for the T^2 range.
[20] R. P. Dickey *et al.*, Phys. Rev. B **56**, 11169 (1997).
[21] This anomaly is similar to the upturn observed in the resistivity of UPt$_3$ in transverse fields, where such a deviation from T^2 behavior at low temperatures is attributed to the fact that the $\omega_c \tau > 1$ limit is realized [22]. In this limit, the characteristic time of the quasiparticle orbital motion is short compared with the time between collisions, and therefore the Fermi surface topology plays an important role in determining transport properties. Note that, due to the presence of this upturn, it was necessary to exclude the lowest temperature data from the T^2 fits (for $H > 8$ T). This was accomplished by using the same chi-square minimization routine as described previously, but by also varying the lower temperature bound.
[22] L. Taillefer, F. Piquemal, and J. Flouquet, Physica (Amsterdam) **153C**, 451 (1988); L. Taillefer, J. Flouquet, and W. Joss, J. Magn. Magn. Mater. **76**, 218 (1988).
[23] A. D. Christianson *et al.*, Phys. Rev. B **66**, 054410 (2002).
[24] T. Muramatsu *et al.*, Physica (Amsterdam) **312B**, 140 (2002).
[25] J. Flouquet *et al.*, Physica (Amsterdam) **319B**, 251 (2002).
[26] P. Gegenwart *et al.*, Phys. Rev. Lett. **89**, 056402 (2002); J. Custers *et al.*, Nature (London) **424**, 524 (2003).
[27] T. P. Murphy *et al.*, Phys. Rev. B **65**, 100514(R) (2002).
[28] T. Tayama *et al.*, Phys. Rev. B **65**, 180504(R) (2002).
[29] A. Bianchi *et al.*, Phys. Rev. Lett. **89**, 137002 (2002).
[30] T. Moriya and K. Ueda, Adv. Phys. **49**, 555 (2000); A. Rosch, Phys. Rev. B **62**, 4945 (2000).
[31] M. D. Daybell and W. A. Steyert, Phys. Rev. Lett. **18**, 398 (1967); E. T. Hedgcock *et al.*, *ibid.* **20**, 457 (1968); H. Rohrer, Phys. Rev. **174**, 583 (1968); P. Monod, Phys. Rev. Lett. **19**, 1113 (1967); R. More and H. Suhl, *ibid.* **20**, 500 (1968); M. T. Béal-Monod and R. A. Weiner, Phys. Rev. **170**, 552 (1968).
[32] U. Rauchschwalbe, F. Steglich, and H. Rietschel, Physica (Amsterdam) **148B**, 33 (1987).
[33] A. Bianchi *et al.*, Phys. Rev. Lett. (to be published).